# **Warming Up Neural Network Basics**

**Cornell CS 5740: Natural Language Processing Yoav Artzi, Spring 2023**

# **Table of Contents**

- A very quick introduction to neural networks
- Architecture basics and matrix notation
- Some practical tips
- Computation graphs

### **A Little Bit of History Neural Networks**

- Neural network algorithms date to the 1980s, and design trace their origin to the 1950s
	- Originally inspired by early neuroscience
- Historically slow, complex, and unwieldy
- Now: term is abstract enough to encompass almost any model – but useful!
- Dramatic shift started around 2013-15 away from MaxEnt (linear, convex) to *neural networks* (non-linear architecture, nonconvex)



#### **The Promise Neural Networks**

- Non-neural ML works well because of humandesigned representations and input features
- ML becomes just optimizing weights
- **Representation learning** attempts to automatically learn good features and representations
- **Deep learning** attempts to learn multiple levels of representation of increasing complexity/ abstraction



#### **The Neuron Building Blocks**

- Neural networks traditionally come with their own terminology baggage
	- Some of it is less common in more recent work
- Parameters:
	- Inputs: *xi*
	- Weights:  $w_i$  and  $b$
	- Activation function *f*
- If we drop the activation function, reminds you of something?



### **Hidden Layers Building Blocks**

- It gets interesting when you connect and stack neurons
- This modularity is one of the greatest strengths of neural networks
- Input vs. hidden vs. output layers
- The activations of the hidden layers are the learned representation





 $h_1 = a_1 W'_{11} + a_2 W'_{21} + a_3 W'_{31} + b'_1$  $h_4 = a_1 W'_{14} + a_2 W'_{24} + a_3 W'_{34} + b'_4$  $h_2 = a_1 W'_{12} + a_2 W'_{22} + a_3 W'_{32} + b'_1$  $h_3 = a_1 W'_{13} + a_2 W'_{23} + a_3 W'_{33} + b'_1$ 



$$
o_1 = h_1 W_{11}'' + h_2 W_{21}'' + h_3 W_{31}'' + h_4 W_{41}'' + b_1''
$$
  

$$
o_2 = h_1 W_{12}'' + h_2 W_{22}'' + h_3 W_{32}'' + h_4 W_{42}'' + b_2''
$$

 $h_1 = a_1 W'_{11} + a_2 W'_{21} + a_3 W'_{31} + b'_1$  $h_4 = a_1 W'_{14} + a_2 W'_{24} + a_3 W'_{34} + b'_4$  $h_2 = a_1 W'_{12} + a_2 W'_{22} + a_3 W'_{32} + b'_1$  $h_3 = a_1 W'_{13} + a_2 W'_{23} + a_3 W'_{33} + b'_1$ 

 $h = aW' + b'$  $\mathbf{o} = \mathbf{h}\mathbf{W}'' + \mathbf{b}''$  $=$   $(aW' + b')W'' + b''$ 



$$
o_1 = h_1 W_{11}'' + h_2 W_{21}'' + h_3 W_{31}'' + h_4 W_{41}'' + b_1''
$$
  

$$
o_2 = h_1 W_{12}'' + h_2 W_{22}'' + h_3 W_{32}'' + h_4 W_{42}'' + b_2''
$$

 $h_1 = a_1 W'_{11} + a_2 W'_{21} + a_3 W'_{31} + b'_1$  $h_4 = a_1 W'_{14} + a_2 W'_{24} + a_3 W'_{34} + b'_4$  $h_2 = a_1 W'_{12} + a_2 W'_{22} + a_3 W'_{32} + b'_1$  $h_3 = a_1 W'_{13} + a_2 W'_{23} + a_3 W'_{33} + b'_1$ 



$$
o_1 = h_1 W_{11}'' + h_2 W_{21}'' + h_3 W_{31}'' + h_4 W_{41}'' + b_1''
$$
  

$$
o_2 = h_1 W_{12}'' + h_2 W_{22}'' + h_3 W_{32}'' + h_4 W_{42}'' + b_2''
$$

$$
h = aW' + b'
$$
  
\n
$$
o = hW'' + b''
$$
  
\n
$$
= (aW' + b')W'' + b''
$$
  
\n
$$
a \in \mathbb{R}^{1 \times 3}
$$
  
\n
$$
W' \in \mathbb{R}^{3 \times 4}
$$
  
\n
$$
W'' \in \mathbb{R}^{4 \times 2}
$$
  
\n
$$
b' \in \mathbb{R}^{1 \times 4}
$$
  
\n
$$
b' \in \mathbb{R}^{1 \times 2}
$$
  
\n
$$
b \in \mathbb{R}^{1 \times 2}
$$
  
\n
$$
o \in \mathbb{R}^{1 \times 2}
$$

#### **Activation Functions Building Blocks**

Activation (non-linearity) function is an entry-wise function *f* : ℝ → ℝ



#### **Probabilistic Outputs Building Blocks**

- What if we want the output to be a probability distribution over possible outputs?
	- So far: output are just real numbers
- Normalize the output activations o using softmax
- Assume your want a distribution over  $y_1, ..., y_n$  (i.e.,  $p(y_i)$ )

$$
\mathbf{o} = \begin{pmatrix} o_1 \\ o_2 \\ \vdots \\ o_n \end{pmatrix} \qquad y = \text{softmax}(\mathbf{o})
$$

$$
p(y_i) = \text{softmax}(\mathbf{o}_i) = \frac{\mathbf{e}^{o_i}}{\sum_{j=1}^{n} \mathbf{e}^{o_j}}
$$

- Essentially: (1) make the value positive; and (2) normalize
- Usually: no non-linearity before the softmax

#### **One-hot Word Representations Building Blocks**

- So far, words (and features) are atomic symbols:
	- "hotel", "conference", "walking", "\_\_\_ing"
- But neural networks take continuous vector inputs
- How can we bridge this gap?
- One-hot vectors

 $\text{hotel} = [0 \ 0 \ 0 \ \cdots 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0]$ conference =  $[0 \ 0 \ 0 \ \cdots 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$ 

- Dimensionality: size of the vocabulary
	- Can be >10M for web-scale corpora
- Problems?

# **Building Blocks**

#### **One-hot Word Representations**

• One-hot vectors

 $\text{hotel} = [0 \ 0 \ 0 \ \cdots 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0]$  $\text{conference} = [0 \ 0 \ 0 \ \cdots 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$ 

- Problems?
	- Information sharing? "hotel" vs. "hotels"

#### **Word Embeddings Building Blocks**

- Each word is represented using a dense low-dimensional vector
	- Low-dimensional << vocabulary size
- If trained well, similar words will have similar vectors
- How to train? What objective to maximize?
	- As part of task training (e.g., supervised training)
	- Pre-training (more on this later)

# **Training Neural Networks**

- No hidden layer  $\rightarrow$  supervised
	- Just like perceptron, but gradient based
- With hidden layers:
	- Latent units  $\rightarrow$  not convex
	- What do we do?
		- ‣ Back-propagate the gradient
		- ‣ Based on the chain rule
		- ‣ About the same, but no guarantees

- One of the most basic neural models
- Example: sentiment classification
	- Input: text document
	- Classes: very positive, positive, neutral, negative, very negative
- We discussed doing this with a bag-of-words feature-based model
- What would be the neural equivalent?

- One of the most basic neural models
- Example: sentiment classification
	- Input: text document
	- Classes: very positive, positive, neutral, negative, very negative
- We discussed doing this with a bag-of-words feature-based model
- What would be the neural equivalent?
	- Concatenate all vectors?

- One of the most basic neural models
- Example: sentiment classification
	- Input: text document
	- Classes: very positive, positive, neutral, negative, very negative
- We discussed doing this with a bag-of-words feature-based model
- What would be the neural equivalent?
	- Concatenate all vectors?
		- $\rightarrow$  Problem: different documents  $\rightarrow$  different input length
	- Instead: sum, average, etc.

#### **Deep Averaging Networks (Iyyer et al. 2015)**



#### **IMDB Sentiment Analysis**



\*It's not common to put nonlinearity before a softmax

# **Classify Word Pair**



- Goal: build a classifier that given a pair of words, classify if they are the full name of a person or not
- The classifier is a multi-layerperceptron with three layers
- Make a drawing!
- Write the matrix notation, including dimensionality of matrices (choose as you wish, and as needed)
- What are the parameters to be learned

Inputs:  $x_l, x_r$ |Input vocabulary:  $\mathscr V$ Embedding function:  $\phi : \mathcal{V} \to \mathbb{R}^{256}$  $W$ eight matrices:  $\mathbf{W}^1, \mathbf{W}^2, \mathbf{W}^3$ Bias vectors:  $\mathbf{b}^1$ ,  $\mathbf{b}^2$ ,  $\mathbf{b}^3$ **Operations:**  $2 \times \sigma : \mathbb{R}^* \to \mathbb{R}^*.1 \times \text{softmax}$ 

# **Practical Tips**

- If you control the model (i.e., not using a pre-trained model)
	- Select network structure appropriate for the problem
		- ‣ Window vs. recurrent vs. recursive (will discuss throughout the semester)
	- Parameter initialization
	- Model is powerful enough?
		- ‣ If not, make it larger
		- ‣ Yes, so regularize, otherwise it will overfit
- Gradient checks to identify bugs
	- If you build from scratch
- Know your non-linearity function and its gradient
	- Example  $tanh(x)$

$$
\frac{\partial}{\partial x}\tanh(x) = 1 - \tanh^2(x)
$$



### **Debugging Practical Tips**

- Verify value of initial loss when using softmax
- Perfectly fit a single example, then mini-batch, then train
- If learning fails completely, maybe gradients stuck
	- Check learning rate
	- Verify parameter initialization
	- Change non-linearity functions

#### **Avoid Overfitting Practical Tips**

- Very expressive models, can overfit easily
	- It will look great on the training data, but everything else will be terrible
- Some potential cures  $\bigoplus$ 
	- Reduce model size (but not too much)
	- L1 and L2 regularization
	- Early stopping (e.g., patience)
	- Learning rate scheduling
	- Dropout (Hinton et al. 2012)
		- ‣ Randomly set 50% of inputs in each layer to 0

# **Computation Graphs**

- The descriptive language of deep learning models
- Functional description of the required computation
- Can be instantiated to do two types of computation:
	- Forward computation
	- Backward computation

#### expression:

*y* = x>Ax + b *·* x + *c*

graph:

### A **node** is a {tensor, matrix, vector, scalar} value



 $\overline{\phantom{a}}$  *pointers to nodes.* expose An **edge** represents a function argument (and also data dependency). They are just

dae's t A **node** with an incoming **edge** is a **function** of that edge's tail node.

A **node** knows how to compute its value and the *value of its derivative w.r.t each argument (edge) times a derivative of an arbitrary input*  $\frac{\partial \mathcal{F}}{\partial f(\mathbf{u})}$ .



#### $\mathbf{x}^{\top} \mathbf{A}$ expression:

graph:

Functions can be nullary, unary, binary, … *n*-ary. Often they are unary or binary.



#### $\mathbf{x}^\top \mathbf{A} \mathbf{x}$ expression:

graph:



Computation graphs are directed and acyclic (usually)

#### $\mathbf{x}^\top \mathbf{A} \mathbf{x}$ expression:

graph:



#### $\mathbf{x}^\top \mathbf{A} \mathbf{x} + \mathbf{b} \cdot \mathbf{x} + c$ expression:



$$
\begin{aligned}\n\text{expression:} \\
y &= \mathbf{x}^\top \mathbf{A} \mathbf{x} + \mathbf{b} \cdot \mathbf{x} + c\n\end{aligned}
$$



variable names are just labelings of nodes.

#### **Algorithms Computation Graphs**

- **• Graph construction**
- **• Forward propagation** 
	- Loop over nodes in topological order
		- $\sim$  Compute the value of the node given its inputs
	- *Given my inputs, make a prediction (or compute an "error" with respect to a "target output")*
- **• Backward propagation** 
	- Loop over the nodes in reverse topological order starting with a final goal node
		- ‣ Compute derivatives of final goal node value with respect to each edge's tail node
	- *How does the output change if I make a small change to the inputs?*

















#### **Draw the Computation Graph MLP**

$$
\mathbf{h}^{1} = \sigma([\phi(x_{l}); \phi(x_{r})] \mathbf{W}^{1} + \mathbf{b}^{1})
$$

$$
\mathbf{h}^{2} = \sigma(\mathbf{h}_{1} \mathbf{W}^{2} + \mathbf{b}^{2})
$$

$$
\mathbf{p} = \text{softmax}(\mathbf{h}^{2} \mathbf{W}^{3} + \mathbf{b}^{3})
$$

# **Constructing Graphs**

#### **Two Software Models**

- Static declaration
	- Phase 1: define an architecture (maybe with some primitive flow control like loops and conditionals)
	- Phase 2: run a bunch of data through it to train the model and/or make predictions
- Dynamic declaration (a.k.a define-by-run)
	- Graph is defined implicitly (e.g., using operator overloading) as the forward computation is executed
	- Graph is constructed dynamically
	- This allows incorporating conditionals and loops into the network definitions easily

# **Batching**

- Two senses to processing your data in batch
	- Computing gradients for more than one example at a time to update parameters during learning
	- Processing examples together to utilize all available resources
- CPU: made of a small number of cores, so can handle some amount of work in parallel
- GPU: made of thousands of small cores, so can handle a lot of work in parallel
- Process multiple examples together to use all available cores

# **Batching**

- Relatively easy when the network looks exactly the same for all examples
- More complex with language data: documents/sentences/words have different lengths
- Frameworks provide different methods to help common cases, but still require work on the developer side
- Key concept is broadcasting: <https://pytorch.org/docs/stable/notes/broadcasting.html>

#### **Batching MLP Sketch**



#### **Batching Rough Notation Sketch**



$$
\mathbf{X}^{(j)} = [x_1, ..., x_{n^{(j)}}], x_i \in 1, ..., |\mathcal{V}|
$$
  
\n
$$
\mathbf{a} = \frac{1}{|\mathbf{X}^{(j)}|} \text{sum} (\phi(\mathbf{X}^{(j)}))
$$
  
\n
$$
\mathbf{h}_1 = \sigma(\mathbf{W}_1 \mathbf{a} + \mathbf{b}_1)
$$
  
\n
$$
\mathbf{h}_2 = \mathbf{W}_2 \mathbf{h}_1 + \mathbf{b}_2
$$
  
\n
$$
p = \text{softmax}(\mathbf{h}_2)
$$
  
\n
$$
\mathbf{X}^{(j)} = [x'_1, ..., x'_M], x'_i = \begin{cases} x_i & i \le n^{(j)} \\ 0 & \text{else} \end{cases}
$$
  
\n
$$
\mathbf{B} = [\mathbf{X}^{(j)}, ..., \mathbf{X}^{(j+B)}]
$$
  
\n
$$
\mathbf{a} = [\frac{1}{n^{(j)}}, ..., \frac{1}{n^{(j+B)}}] \text{sum} (\phi(\mathbf{B}))
$$
  
\n
$$
\mathbf{h}_1 = \sigma(\mathbf{W}_1 \mathbf{a} + \mathbf{b}_1)
$$
  
\n
$$
\mathbf{h}_2 = \mathbf{W}_2 \mathbf{h}_1 + \mathbf{b}_2
$$
  
\n
$$
p = \text{softmax}(\mathbf{h}_2)
$$

Not accurate notation, for illustration only

- You have to get certain operations right, such as sum
- But PyTorch's broadcasting sorts out most operations

# **Batching**

#### **Complex Network Architectures**

- Complex networks may include different parts with varying length (more about this later)
- In the extreme, it may be complex to batch complete examples this way
- But: you can still batch sub-parts across examples, so you alternate between batched and nonbatched computations



#### **Documents**



# **Acknowledgements**

- Slides adapted from or inspired by Dan Klein, Dan Jurafsky, Chris Manning, Michael Collins, Luke Zettlemoyer, Yejin Choi, and Slav Petrov
- Some slides were adapted from **Practical Neural Networks for** [NLP](https://github.com/clab/dynet_tutorial_examples) / Chris Dyer, Yoav Goldberg, Graham Neubig / EMNLP 2016